#### Unit-V

- 5. (a) What are the basic components of a general fuzzy controller ? Discuss in detail.
  - (b) Assume that each individual of a group of eight decision makers has a total preference ordering P;
     (i ∈ N<sub>8</sub>) on a set of alternatives X = {w, x, y, z} as follows :

$$P_{1} = \{w, x, y, z\}$$

$$P_{2} = P_{5} = \{z, y, x, w\}$$

$$P_{3} = P_{7} = \{x, w, y, z\}$$

$$P_{4} = P_{8} = \{w, z, x, y\}$$

$$P_{6} = \{z, w, x, y\}$$

### (A) of Then (A) and subcassion $\{0, 2, 3, 5\} > x$

- (i) Find the fuzzy preference ordering relations.
- (ii) Also find  $\alpha$ -cuts of this fuzzy relation S and group level of agreement concerning the social choice denoted by the total ordering  $\{w, z, x, y\}$ .
- (c) Solve the following fuzzy linear programming problem :
- Max.: view isobardow :  $\begin{cases} x_1 + y_2 \\ y_1 + y_2 \\ y_2 \end{bmatrix} = 6x_1 + 5x_2$  is the formula of the f

s. t. :  

$$(5,3,2)x_1 + (6,4,2)x_2 \le (25,6,9)$$

$$(5,2,3)x_1 + (2,1.5,1)x_2 \le (13,7,4)$$

$$x_1, x_2 > 0.$$
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 $X = \{0, 2, 4, 5, \dots, 80\}$ 

idempotent t-trans. Also prove that (al. a while (c.) is a dual triple where (c.) is the acai comoistnent.

# M. A./M. Sc. (Final) EXAMINATION, 2020

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#### MATHEMATICS

(Optional)

Paper Fifth (iii)

(Fuzzy Sets and Their Applications)

Time : Three Hours

#### Maximum Marks : 100

Note: Attempt any *two* parts from each question. All questions carry equal marks.

1. (a) Prove that a Fuzzy set A on R is convex iff:

 $A(\lambda x_1 + (1 - \lambda) x_2) \ge \min[A(x_1), A(x_2)]$ 

for all  $x_1, x_2 \in \mathbb{R}$  and all  $\lambda \in [0, 1]$  where min denotes the minimum operator.

(b) Let  $f: X \to Y$  be an arbitrary crisp function. Then for any  $A \in F(\alpha)$  and all  $\alpha \in [0,1]$  prove that (f fuzzified by the extension principle)  $\alpha [f(A)] \supseteq f({}^{\alpha}A)$  but not conversely.

(A-53) P. T. O.

- (c) Prove that the standard fuzzy intersection is the only idempotent *t*-norm. Also prove that  $(ab, a + b ab, (c_s)$  is a dual triple where  $(c_s)$  is the standard complement.
- 2. (a) Calculate the fuzzy cardinality and scalar cardinality of the fuzzy set defined by A :  $X \rightarrow [0, 1]$ , where  $X = \{0, 2, 4, 6, \dots, 80\}$  and :

$$A(x) = \begin{cases} 0 & \text{if } x \le 20 \text{ or } x \ge 60 \\ (x-20)/15 & \text{if } 20 < x < 35 \\ (60-x)/15 & \text{if } 45 < x < 60 \\ 1 & \text{if } 35 \le x \le 45 \end{cases}$$

(b) Let A ∈ F(R). Then prove that A is a fuzzy number iff there exists a closed interval [a, b] ≠ φ such that :

$$A(x) = \begin{cases} 1 & \text{for } x \in [a, b] \\ l(x) & \text{for } x \in (-\infty, a) \\ r(x) & \text{for } x \in (b, \infty) \end{cases}$$

where *l* is a function from  $(-\infty, a)$  to [0,1] that is monotonic increasing, continuous from the right and such that l(x) = 0 for  $x \in (-\infty, w_1)$  and *r* is a function from  $(b,\infty)$  to [0,1] that is monotonic decreasing, continuous from the left and such that r(x) = 0 for  $x \in (w_2, \infty)$ .

(c) Find the transitive max-min closure  $R_T$  for a fuzzy relation defined by the following membership matrix :

$$\mathbf{R} = \begin{bmatrix} .8 & .6 & 0 & 0 \\ 1 & 0 & 1 & 1 \\ .2 & .4 & 0 & 0 \\ 0 & 0 & .9 & .8 \end{bmatrix}$$

A-53) P. T. O.

#### Unit—III

## 3. (a) Solve $p \circ Q = r$ , where : $\begin{bmatrix} .1 & .4 & .5 & .1 \end{bmatrix}$

- $Q = \begin{bmatrix} .9 & .7 & .2 & 0 \\ .8 & 1 & .5 & 0 \\ .1 & .3 & .6 & 0 \end{bmatrix} \text{ and } r = [ .8.7.50 ]$ 
  - (b) Prove that :

$$Pl(A) \ge Bel(A)$$

for all  $A \in P(X)$ .

- (c) Let a fuzzy set F be defined on N by F = .4/1 + .7/2 + 1/3 + .8/4 + .5/5 and A(x) = 0 for all x ∉ {1,2,3,4,5}. Determine Nec (A) and Pos (A) induced by F for all A ∈ P ({1, 2, 3, 4, 5}).
  Unit—IV
- 4. (a) Write short notes on the following :
  - (i) Multivalued logic
  - (ii) Linguistic hedges
  - (b) Let sets of values of variables x and y be  $X = \{x_1, x_2, x_3\}$  and  $Y = \{y_1, y_2\}$ , respectively. Assume that a proposition "if x is A, then y is B" is given, where  $A = .5/x_1 + 1/x_2 + .6/x_3$  and  $B = 1/y_1 + .4/y_2$ . Then, given a fact expressed by the proposition "x is A'," where  $A' = .6/x_1 + .9/x_2 + .7/x_3$ . Use the generalized modus ponens to derive a conclusion in the form "y is B'."
  - (c) Write the reasonable axioms of fuzzy implications.

(A-53) P. T. O.

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